

# An Alternate Form of the Integrated First-Order Rate Equation

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## Abstract

Derivation of a first-order equation suitable for use in beginning energy science and chemistry courses is shown to be

$$A = A_o / 2^{t/t_{1/2}}$$

Where,

$A_o$  is the original amount of the sample

A is the amount

T is time t and

$t_{1/2}$  is the half-life

$A_o$  is larger than A

## Derivation of the Alternate Form

Radioactive processes and many chemical processes follow first order kinetics. The usual equations

found in general chemistry textbooks are:

- $\ln A_o / A = kt$ , Where,  $A_o$  is the original amount of the sample, A is the amount at time t and k is the rate constant.
- Changing the rate constant to half-life,  $\ln 2 = kt_{1/2}$ , where  $t_{1/2}$  is the half-life.
- Solving equation 2 for k and substituting into equation 1 the result is  $\ln A_o / A = (\ln 2)t / t_{1/2}$ .
- Rearranging equation 3 gives  $A = A_o / e^{(\ln 2)t/t_{1/2}}$  as indicated in [1].
- Since  $e^{\ln 2} = 2$ , substitution into equation 4 yields  $A = A_o / 2^{t/t_{1/2}}$  the Alternate Form of the

## Integrated first-order rate equation

Our students have found equation 5 to be relatively easier to use than equations 1 and 2. In equation 5, by dividing the time by the half-life, they get a number. On their calculators, they enter the number 2, y<sup>x</sup>, the number and press = The result is divided into  $A_o$ , giving the value for A. For radioactive processes, the values of  $A_o$  and A may be in mass, such as grams, or activity in Becquerel's (counts/second). For chemical processes, units for  $A_o$  and A may be written as rates, such as molarity/second.

## References

- Kenneth AC (1991) Chemical kinetics, the study of reaction rates in solution. VCH Publishers, USA, p. 496.

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