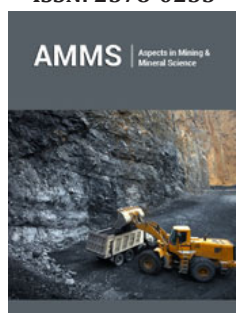



Most Common Misprints in Definitions of Zeldovich Number Fatally Affecting Preliminary Estimates of Combustion Thermal Activity

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Opinion

Any investigation concerning experimental data or computer modeling needs that the preliminary estimates have been already done. In the case of combustion thermal activity these estimates are based inevitably on the well-known Zeldovich number (Ze). Nevertheless, it turns out, that the existing Ze definitions are strongly different both from each other and from the correct version of them [1-3]. In the paper presented let's consider the most common misprints in definitions of Ze and explain the contradictory conclusions they lead to. In accordance with the electronic encyclopedia (Wikipedia 2025) the first definition of Zeldovich number has been published in proceedings of the ICDERS meeting [4], at Poitiers

1983: $\beta = \frac{E_a}{RT_b} \frac{(T_b - T_u)}{T_b}$ (1). Actually, β is the wave parameter providing its existence (at $\beta \ll 1$, $\gamma \ll 1$, see Table 1)

where,

β has been supposed to be the Ze number, while

E_a is the activation energy,

T_b is a burnt gas temperature,

T_u is an unburnt gas temperature.

Nevertheless, even earlier Zeldovich himself has written in his famous book (1) the following expression as definition of his number (introduced as z in the book): $Ze = \frac{E_a}{RT_b} \frac{(T_b - T_0)}{2RT_b^2}$ (2),

At the same time A.G. Merzhanov in his monography (2) uses the adiabatic temperature T_{ad} instead of the actual combustion temperature T_b (see (2)): $Ze = \frac{E_a}{RT_b} \frac{(T_{ad} - T_0)}{2RT_{ad}^2}$ (3). To illustrate the huge difference between expressions (2) and (3) leading to completely contradictory conclusions, let's consider the hydrogen-oxygen flame stability. It is well-known that there is practically no difference between T_b and T_{ad} in turbulent combustion [5-7]. In combustion synthesis T_{ad} corresponds to the complete conversion, while T_b may be related with an incomplete transformation of the initial components [8]. Correspondingly, the turbulent combustion of premixed hydrogen-oxygen mixtures is absolutely stable ($Ze < Ze_{cr} = 2 + \sqrt{5}$)

while vice versa the hydrogen-oxygen flame with an incomplete conversion ($Ze \geq Ze_{cr} = 2 + \sqrt{5}$) oscillates and demonstrates unstable propagation (see [3]). Thus, one have to understand that correct

definition of Ze is described by the expression (2) only. The work presented above has been done under the state assignment for ISMAN (125021201988-9).

Table 1: Combustion reactions and the conditions of their activation.

1	Reaction/Production	E_a , kJ/mole	T_{ad} , K	Note, Conditions	Ze	$\beta=$, $\gamma=$
2	Zn+S in Argon	34	1916-2609	In Argon	0.69-0.89	0.5, 0.6
3	Zn+S in Air	275	5043-6768	In Air	3.08-2.33	0.04, 0.05
4	Ni+Al	1,55,159	3750	Not activated mechanically	2.35	0.04, 0.05
5	Ni+Al	50,80		Mechanically activated	1.18	0.04, 0.05
6	Ti+C in Argon	364	$1000 < T_{ad} < T_{melt}$ $T_i = 1948$		79.04	0.04, 0.05
7	Sphalerite in Air (S)	275	$1000 < T_{ad} < T_{melt}$ $S = 1293$		9.8	0.04, 0.05
8	Wurtzite in Air (W)	275	$T_{ad} < T_{melt}$, $W = 1991$		7.05	0.06, 0.07
	C_2H_2 +Air	150	$T_{ad} \leq 2395K$	On Pd catalyst	> 4.2428	
	C_2H_2 +Air	150	$T_{ad} \geq 2397K$	On Pd catalyst	< 4.2387 53	
	Ti+C in Argon	364	$T_{ad} < T_{boil}$, $T_i = 3440K$		48.29	> 0.5 , > 0.6
	Hf+N ₂	375	$T_{ad} < T_{melt}$, $H_f = 2495K$		7.95	
	Hf+N ₂	375	$T_{ad} = 5100K$		4.161	> 0.5 , > 0.6
	Zr+N ₂ , ZrN	192	$1873 < T_{ad} < 2123 < T_{melt}$, ZrN		4.74	0.067, 0.080
	Zr+N ₂ , Solid Solution of N ₂ in Zr (SSN)	234	$T_{ad} < 1873 < T_{melt}$, SSN ~ 2128		6.42	0.080, 0.095
	Zr+O ₂ , ZrO ₂	118-210	$2128 \sim T_{ad} < 2988$ $= T_{melt}$, ZrO ₂	In Oxygen	2,86-5.098	

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