

Behaviour of Geometrically Nonlinear Columns: Towards an Accurate Structural Design of Columns Made Using Hot Rolled-Open Steel Section

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Abstract

Geometrically nonlinear columns have been used for a variety of reasons in buildings, and their use has become even more prevalent in our time. Much research has been carried out regarding columns and arches, but geometrically nonlinear columns have not been extensively covered. Thus, this paper sheds a light on the behaviour of nonlinear columns when subjected to loading. For that purpose, two different cases of geometrical nonlinearities were considered. These columns were modelled using a validated Finite Element (FE) model. Each of the columns was loaded up to the buckling load and the displacement was recorded. Length of the column, the included angle (i.e., shallowness or span/reach ratio) and boundary conditions were taken as variables and the behaviour of columns noted each time. Additionally, a brief review of the available guidance from building codes showed a gap when it comes to nonlinear steel columns design. The results of this study showed a similarity between these columns and arches in terms of their behaviour up to the point of buckling. A parametric study was also performed to highlight the sensitivity of this hypothesis to changes in the studied parameters.

Keywords: Buckling; Compression; Flexure; Geometrically Nonlinear Columns; In-plane buckling; Open steel sections; Out of plane buckling

Introduction

Generally, columns transfer applied loads through compression. Other types of stresses (such as flexural and torsional) also do form in columns, especially columns in use within a structure rather than those erected in a laboratory setting for testing purposes. The nature of the stresses developing in columns varies widely depending on several factors such as the type of building where the column is erected, the type of the column connections (i.e., a simple column or a fixed-end column), the material of which the column is made of, the effective length, the nature of loads being applied, etc. To this end, various publications and research have been carried out discussing and observing the behaviour of columns for each of the mentioned factors. However, the nature of column usage has been changing and with that, it becomes necessary to do more research into how columns respond to these changes. With the ever more growing size of the urban areas and the emerging need for building to do far more than just carry the loads that they are designed for, the demand for unusual and nonlinear structures has become something that the modern-day construction sector just cannot do away with. Thus, one of the main members of the structure that has been widely affected by this is columns (e.g., using arch columns instead of the linear columns).

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Formulas enabling the determination of buckling loads have been discussed at length, including the loading, material and geometrical imperfections [1-4]. These imperfections, though, are unintended and tend to be small in value or consequences. Other researchers have investigated factors that affect column capacity during accidents such as fire [5-7].

Further studies have shown that columns and arches behave somewhat similarly when subjected to a set of loading. Komatsu [8,9] found that normal column curves could be used to accurately estimate the thrust at quarter points of arches, after correction for effective length, yield strength and other parameters. It is also known that all steel structures which are curved in elevation are recommended to be designed, at least partially, as arches [3,10,11]. It is observed that arches develop similar internal stresses to that of columns when loaded and fixed in a certain position [1,8,9].

At the early stages of studying nonlinear elements, it was assumed that pre buckling deformation was of minor significance, and that classic theory of buckling could be used to estimate the load-carrying capacity of geometrically nonlinear elements due to similarities between arches and column behaviour [8,9]. However, other studies [1,12-14] observed that for shallow arches, these pre buckling deflections were quite significant. As such, using the classic theory of buckling would lead to an overestimation of the load-carrying capacity of these elements. Other studies have further considered the behaviour of arches under different sets of loading applied in different ways [8,14-19].

Another phenomenon that affects the design of arches to a great degree, is out of plane buckling [2,4,11, 20-26]. For arches to be able to effectively carry the applied loads, this mode of failure should be prevented. If not, this will lead to a loss of stability and the structure could potentially collapse before reaching its design load. These research still don't make an explicit connection between behaviour of arches and nonlinear columns.

Although the amount of research carried out regarding linear columns and arches are extensive, studies about the behaviour of nonlinear columns when subjected to loading are very scarce. The design guidance available [3,10,11] recommend using the equations that are developed for arches to get a rough estimate of the load-carrying capacity of the curved steel members (including columns). Various cases of buckling have been discussed for columns, arches and ring structures in the publicly available literature [20], but not nonlinear columns [21-26].

Moreover, the beam-column theory has been investigated in depth by several researchers [15,27-30]. This has been particularly useful to study the effects of elements where flexural and axial forces are present simultaneously. Design checks can be found in the design guides that allow for accurately estimating the load-carrying capacity of structural elements when they are subjected to this type of loading. This theory, though, cannot explain the behaviour of columns that are purposefully geometrically nonlinear.

Furthermore, Thin-walled structures with geometric nonlinearities have been investigated [31-33] but the difference

between thin-walled closed sections and regular steel sections is large. A wide range of studies can be found on the nonlinear behaviour of structural elements arising from filling closed steel sections with concrete (i.e., Material nonlinearity) [34-37].

The effects of geometric nonlinearity for Reinforced Concrete (RC) columns have been studied [38] namely on the load-carrying capacity of such columns, among other things. Free vibration and stability of steel columns with geometric nonlinearity have been discussed in detail [39]. There is, however, a gap in the literature regarding the effects of geometric nonlinearity on the pre buckling load-carrying capacity of steel columns.

The purpose of this paper, therefore, would be to study the behaviour of geometrically nonlinear steel columns under a set of loading conditions or / types, and to establish a relationship between the applied loads and the deformation of such columns. This would pave the way for driving specific formulas for accurately estimating the correct load capacity of nonlinear columns. Another reason of this study is to allow structural designers to consider the use of geometrically nonlinear columns as structural elements rather than view them as purely architectural, which enables a more cost-effective design for any potential clients.

This paper aims to achieve its objectives by undertaking a parametric study into the effects of geometrical nonlinearity on the behaviour of columns. The parameters are length of the column, included angle and boundary conditions. A Finite Element (FE) model is established and validated against the experimental programme handled by previous research [21] in the fourth section of this paper. This validated FE model is used to establish the results of the parametric study. In section five, the results are discussed and used to shine a light on the current design guidance by comparing the guidance to the findings of this paper. Future areas for potential studies are highlighted in this section as well. Concluding remarks are mentioned in section six along with a brief overview of the current guidance and how can they be improved upon.

The parametric study takes into account one variable at a time to establish a clear picture of how each factor affects the column behaviour under loading. The results are then established by comparing the obtained data from the validated FE model.

Methodology

The geometric nonlinearities considered in this paper are curved columns and columns with a Y shape. These columns are not to be confused with linear non-straight columns as the effects of the geometrical nonlinearity of the earlier varies along the length of their profile.

An FE model was set up using Abaqus to investigate the effects of such geometrical nonlinearity to test this theory. This model was validated by comparing the results obtained from the FE model to an experimental study [21] which was carried out to investigate the out-of-plane and in-plane buckling of free-standing arches using hot-rolled open steel sections. The validation results are discussed at length in the next section.

The validated FE model is utilized to carry out a parametric study into 3 different factors affecting the behaviour of geometrically nonlinear columns. These factors are length of the column, included angle and boundary conditions. The factors have been shown to have significant impacts on the behaviour of similar structures in the available literature [26,40].

In the first case, a curved column was considered. Each of the factors mentioned above were studied as follows (i-iii):

i. Length: 3 different lengths were considered. In each case the boundary conditions were modelled so that the bottom end of the column was pinned, and the upper end was free to move vertically, but otherwise restrained. The included angle was kept constant at 45 degrees. The length of the curved columns was taken as 2.77m, 3.20m and 4.16m.

ii. Boundary conditions: 3 cases were studied with each one having a different boundary condition. The length of the column was taken as 3m. The included angle was kept constant at 45 degrees. For the first case, the lower end was pinned, and the top end was modelled as a fixed connection. For the second case, the bottom end was pinned, and the top end was given horizontal movement restraint only. Lastly, the bottom end was fixed, and the top end was made free.

iii. Included angle: In this case, the effects of 3 different angles were studied. The first case was studied with an included angle of 45-degrees. This was then reduced to 35-degrees. Lastly, a 55-degree included angle was considered. The length of the curved column was taken as 3m. Boundary conditions was assumed as pinned at the lower end of the column. The top end was free to move vertically, but otherwise restrained (Figure 1).

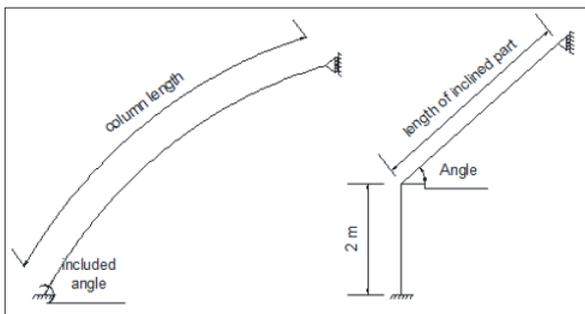


Figure 1: Geometrical nonlinearities considered in the parametric study.

For the second type of column, a single armed Y shape, the same cases were studied as follows (i-iii):

i. Length: for the Y shaped column, only the length of the arm was changed. This was done based on 0.5m incremental. Firstly, the length was taken as 5.41m, then 5.91m and, lastly, 6.41m. The included angle was kept at 45 degrees. Boundary conditions at the lower end of the column was modelled as pinned, whereas the top end of the column was vertically free, but otherwise restrained.

ii. Boundary conditions: 3 cases were studied. Initially the bottom end of the column was modelled as pinned, but the top end

was free vertically and restrained in all other directions. The length and the included angle were kept constant.

iii. Included angle: 3 different angles were studied with 10-degree increments. First off, the included angle was modelled as 40 degrees, then 50 degrees and, lastly, 60 degrees. The boundary conditions for these cases were such that the column was pinned at the lower end, whereas the upper end was modelled to be free vertically, but otherwise restrained.

The buckling load and the displacement of the columns were recorded in each of the cases to allow for the results to be established.

Verification of the FE model

The validation of the model was carried out in two ways.

i. By comparing the results of the model that was created to the results of an experimental study into arches [21]. A model arch was created similar to that which was used for the purpose of the experimental study. The similar loading phase that was applied in the test implemented into the model. Figure 2 shows a comparison of the results between the recorded displacement at the top of the arch in the model and that of the experimental study.

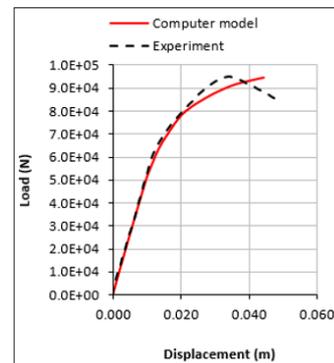


Figure 2: Load-Displacement curve comparison between FE model and Experimental study [21].

ii. Using the FE model, the stress-strain relationship was drawn as shown in Figure 3. The results closely matched those reported in the paper [21].

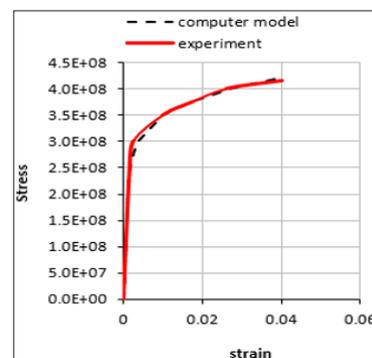


Figure 3: Stress-Strain curve comparison between results obtained from FE model and results obtained from experimental study [21].

The results of the FE model closely matched those of the experimental study. Based on these, the results obtained from the FE model was considered validated.

During the validation of the FE model, it was observed that the displacement of the column was almost twice that of an arch with similar properties and similar geometry. This is due to the fact that an arch, if split at the midpoint, is essentially made up of 2 columns. Hence, it is reasonable for a column, which represents half of an arch to show a displacement that is twice as big as that of the arch under the same load. Based on this, the applied loads on the columns were reduced by half to make them more reflective of the reality of the cases as shown in Figure 4.

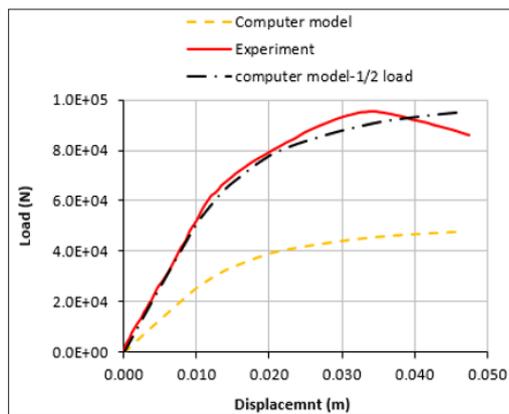


Figure 4: Comparison between displacement values for columns and arches.

During the verifications of the model, a mesh sensitivity analysis was carried out to determine the effects of type of mesh used and the size of it on the eventual outcome of the modelling. Effects of different types of mesh was found to have negligible effects on the modelling of the columns. However, a slight variance could be seen when different mesh sizes were tested. This is shown in Figures 5 & 6. Based on the observation, a mesh size of 0.145mm was chosen. The element type used for this study was shear flexible elements since no significant change could be seen when other types of elements were tried out.

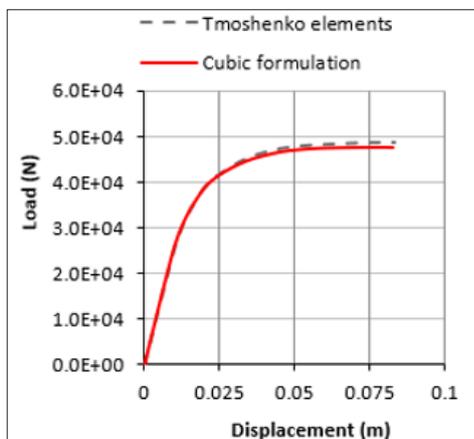


Figure 5: Effects of different types of mesh on the accuracy of the analysis.

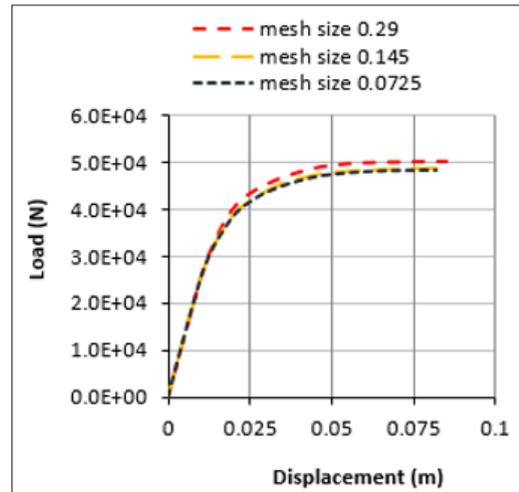


Figure 6: Effects of different sizes of mesh on the accuracy of the analysis.

Results and Discussion

After the validation of the FE model was achieved, the next stage was to conduct the parametric studies to observe the effect of the variables mentioned in the methodology section on geometrically nonlinear columns

The column section that was used in this paper was identical to the sections used in the validation of the FE model [21].

Columns were modelled using the validated FE model and were given the dimensions shown in Figure 7 (HE 100 section). The grade of the steel used for modelling was taken as S235 since these sections are widely used in the construction industry.

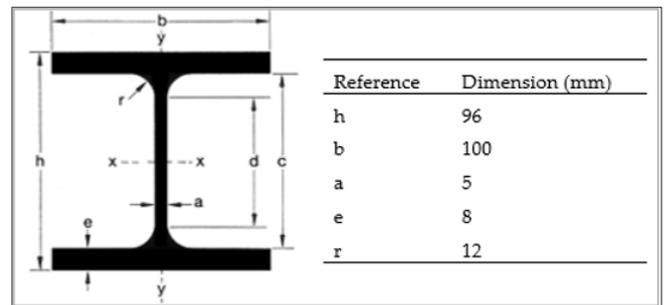


Figure 7: Details of the section used for testing.

Loads were applied up to buckling point at increments of 1% of the original load, which was set to 1kN. Load-displacement was recorded, and the results are shown in the Figures below.

The results shown in Figures 8-13 confirmed the importance of geometrical nonlinearity (among other things) on the eventual load-carrying capacity of columns. The results highlighted how initial geometrical nonlinearities affect the load-carrying capacity of the columns, as has been reported in the literature [13,14, 24,26,32,40,41]. Significant differences were observed in the ultimate capacity of columns depending on whether the column was curved or Y shaped. Further investigation is required to explore this area in future studies.

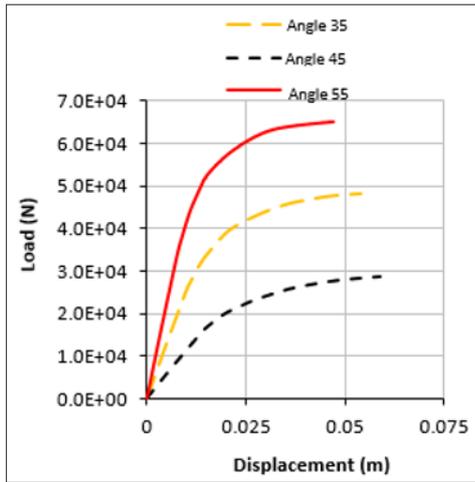


Figure 8: Displacement curve comparison when the included angle is changed.

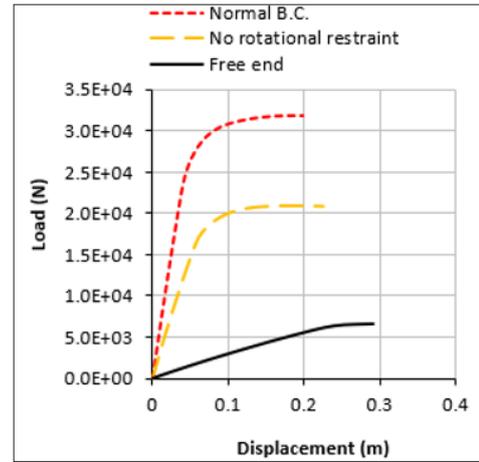


Figure 11: Displacement curve comparison when the boundary conditions of the column is changed.

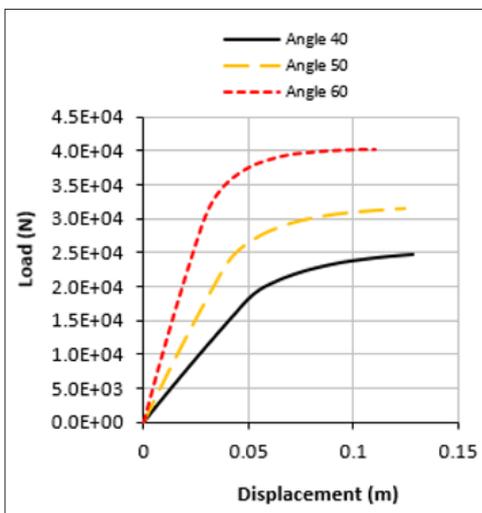


Figure 9: Displacement curve comparison when the included angle of the column is changed.

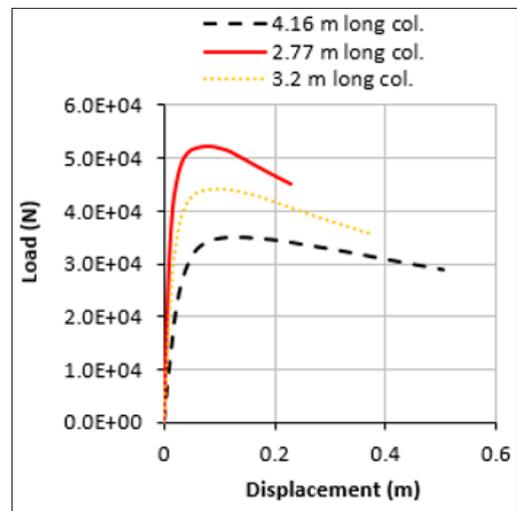


Figure 12: Comparison of displacement curves with when the column length is variable.

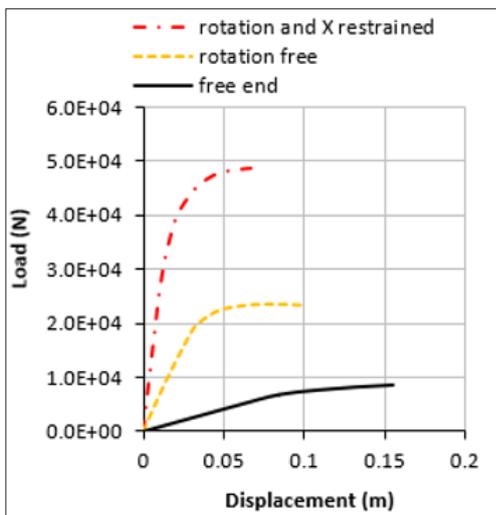


Figure 10: Displacement curve comparison when boundary conditions are variable.

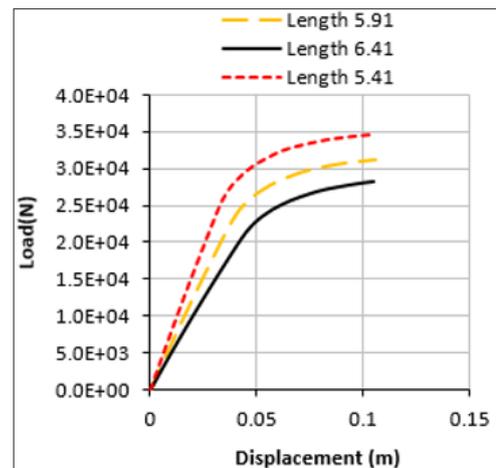


Figure 13: Displacement curve comparison when the length of the column is changed.

The study also shows a clear effect of the included angle on the ultimate value of the load-carrying capacity of the columns.

As seen in Figure 8, changing the included angle for the curved columns from 55 degrees to 35 degrees resulted in a reduction of more than 50% of the load-carrying capacity. This reduction is further confirmed by the results of the Y shaped columns (Figure 9), although a less significant reduction was observed; of 30%. This is in line with what other researchers have found [26,40].

From the results, it was also noticed that the columns started showing nonlinear behaviour at similar stages based on the value of the included angle. Pi et al. [26,40] reported similar observations for the curved columns as shown in Figure 10. The load-displacement curve started exhibiting nonlinear behaviour at roughly 45% of the buckling load. Although the final value of the buckling loads was different for each included angle, the ratio at which the columns started displaying nonlinear behaviour remained roughly the same. For the Y shaped columns, the columns started showing nonlinear behaviour at just over 70% of their buckling loads. This is a stark difference to what was observed in the curved columns.

Furthermore, the results shown for the columns which are not restrained in any direction at the top indicate substantive deformation under small loads. Out of plane buckling was the mode of failure in this scenario (Figures 10 & 11). This finding is in line with the established knowledge that cantilever columns and arches lose a significant amount of load-carrying capacity if out of plane displacement is not restrained [3,11]. However, having a non-restrained column that is geometrically nonlinear in buildings is not very common. That is why all other cases investigated with some form of lateral restraints applied to the top ends of the columns.

Additionally, it can be noticed that that the buckling load values for columns increases with the increase of the included angle. This points to the fact that classical buckling formulas could be used up to a certain point when dealing with geometrically nonlinear columns. Similar findings have been reported in existing literature [8,9] But, as was noticed earlier (Figures 8 & 9), the change in the buckling load value was not linearly proportional to the value of the included angle. Hence, a linear formula for obtaining the buckling load will lead to an overestimation of the actual load-carrying capacity of the column.

La et al. [21] examined freestanding arches for in and out-of-plane buckling. In this paper, all the columns were supported laterally at the top and the load was applied at the top except one case that has been referred to above. This meant that the columns were not susceptible for out-of-plane buckling.

The type of the restraint provided at the top has a remarkable effect on the load-carrying capacity of the columns, as shown in Figures 10 & 11. For the curved columns, when the top end was laterally and rotationally restrained, the ultimate load capacity of the column was measured at around 49kN. When the rotation restraint was removed from this end, the ultimate load was measured at just 23kN. This is a significant drop in the value of the ultimate load-carrying capacity of the column. The observation is also in agreement with the buckling theory and the influence of boundary conditions on load-carrying capacity of columns.

For the single armed Y shaped columns, the reduction of the pre-buckling load was observed to be less severe than it was with curved columns. When the column was laterally and rotationally restrained at the top, the buckling load that was recorded as 32kN. When the boundary condition at the top was changed and rotation was allowed, the value of the load dropped to 21kN.

Another interesting observation was made regarding the effects of the shape of the columns on the pre-buckling behaviour. As it can be seen in Figure 12, the columns reach their ultimate section capacity before the nonlinear behaviour starts to develop. This is almost the case for all the examined specimens. This could be due to the fact that the test specimens which are short columns with max length of 4.16m. Due to that fact, the column fails in compression rather than buckling [3,11,15]. It is, therefore, suggested that any future studies investigate a wide variety of lengths to be able to reach a definitive conclusion.

The results shown for the Y shaped column, though, paint an interesting picture as shown in Figure 13. In this Figure, it can be seen that all the columns start exhibiting nonlinear behaviour before reaching their ultimate load and fail in buckling. Furthermore, all columns, regardless of length, started exhibiting nonlinear behaviour at about 70% of their buckling load. This can be interpreted by the fact that the Y shaped columns were slenderer and were more likely to fail in buckling before reaching their section capacity.

As noted in the first paragraph, this study underlines the importance of carrying out separate investigations into each type independently. Comparing results on two different cases against each other is difficult and might lead to inaccurate conclusions.

It remains to be said that the number of tests carried out was very limited. The parameters that were measured were buckling load and displacement is known that many factors affect the load-carrying capacity of columns as has been shown in the results, regardless of whether these columns are traditional geometrically linear columns or nonlinear ones similar to what has been covered in this paper. Drawing generalised conclusion, hence, will be difficult from this limited study.

Therefore, the authors of this paper recommend further investigation into this subject. Areas that have been identified for future studies are as below:

- i. The effects of different forms of geometrical nonlinearity; this paper investigated only two forms of geometrically nonlinear columns. Other forms should be explored and understood fully before an informed conclusion regarding the design approach could be made.
- ii. This paper considered only open steel sections. Further studies are needed on other types of sections that are commonly used for columns. It is recommended that large scale studies carried out into the behaviour of each type independently, since comparing one type against another may lead to ambiguous and inaccurate conclusions.

iii. Carrying out an experimental study where columns can be fabricated as full-scale columns. This is very beneficial for any future studies in terms of validating FE models that could be used for further investigation. It also provides an important insight into the behaviour of columns since man-fabricated columns have a larger degree of inaccuracy than those examined through FE modelling.

iv. Undertaking further studies to determine the influence of different types of loading on geometrically nonlinear columns. In this paper, only one type of loading was examined. Different kinds of loads are applicable to columns in reality and they may act separately or together on the columns. The effects of such scenarios will have to be investigated further.

v. Any future studies should take into account a wider range for each of the variables considered. This allows researchers to make solid conclusions in light of a bigger pool of data and would be statistically more reliable.

vi. Further studies regarding geometrically nonlinear columns with different types of material; This paper considers the behaviour of steel open sections only. However, A wide range of various materials are used to fabricate/erect columns in the construction industry. This is an area that can be studied further.

As highlighted above, this paper studied only a small number of samples. Thus, developing an appropriate and fully tested design approach based on the results of this study is likely to be inappropriate/inaccurate [41].

However, from the results it can be seen that there is a similarity between the behaviour of geometrically nonlinear columns and arches. With the out-of-plane buckling mode being ruled out by restraining the top end against lateral movement, other parameters such as buckling mode, included angle and length showed similar results to what has been shown in previous studies investigating arches [21]. Therefore, after accounting for appropriate correcting factors, it is possible to utilise the available guidance in different codes of practices to estimate the load-carrying capacity of geometrically nonlinear columns. This, it is emphasised, requires further studies and further testing to be carried out in order to allow for making confident conclusions.

The available design codes ambiguously refer to the effects of geometrical nonlinearity during the design process. In Eurocode [3], the fundamentals formula that is adhered to is the notion that design loads should be less than the design resistance of the columns. This is expressed as below:

$$M_{Ed} \leq M_{N,Rd}$$

Where,

M_{Ed} is applied design moment

$$M_{N,Rd} = M_{pl,Rd} [1 - (N_{Ed} / N_{pl,Rd})^2]$$

$M_{pl,Rd}$ is Plastic moment capacity of the section

$N_{pl,Rd}$ is Squash load of the section

Clause 5.5.4 (1) of the Eurocode 3 provides an interaction formula to cater for the combined effects of axial and flexural stresses

$$\frac{N_{sd}}{X_y A_f} + \frac{K_y M_{y,sd}}{W_{pl,y} J_y} \leq 1.0$$

K_y is a factor to allow for the effects of the secondary moments, non-uniform moments and spread of yield.

$$K_y = 1 - \frac{\mu_y N_{sd}}{X_y A_f} \text{ but } K_y \leq 1.5$$

And

$$\mu_y = \lambda_y (2\beta_{My} - 4) + \frac{w_{pl,y}}{w_{el,y}}$$

with its value bigger not bigger than 0.9

It can be seen from above that the Eurocode vaguely refers to the effects of non-uniform moments on the load-carrying capacity of columns. This, however, does not explicitly account for the effects of nonlinear behaviour of columns which are caused by geometrical nonlinearities, such as depth to span ratio.

The Eurocode does, however, provide charts and design curves to enable the design of arches. These design curves do consider geometrical nonlinearities.

In Annex D.3 of BS EN 1993-2 [11], The formulas for estimating in plane and out of plane buckling loads are given for arches. The formula, unlike those specific to columns, allows for the effects of depth to span ratio. This has been achieved by including a buckling length factor for most common forms of arches.

$$N_{cr} = \left(\frac{\pi}{\beta_s} \right)^2 EI_y$$

N_{cr} is the max compression force at the supports that the arch can support

β_s is buckling length factor which is given in appendix D3.2 in Eurocode 3

The formula above, which is provided in Eurocode 3, is to obtain an estimate of the critical compression load at the supports. As can be seen, the formula allows for the effects of rise/span ration by including the buckling length factor (β_s). The buckling length factor curves is given in appendix D3.2 in Eurocode 3.

Conclusion

Behaviour of geometrically nonlinear columns, despite their wide use in the construction industry, remains vaguely understood as has been outlined in the introduction section of this paper. Design codes and guidance available do not offer explicit formulas to deal with geometrically nonlinear columns; but rather a design approach for members which are curved in the plane of the load [3,10,11]. These formulas could be used to estimate the load-carrying capacity of arches accurately considering that they have been developed for arches. The authors of this paper are concerned that using these formulas could lead to an over estimation of the load-carrying capacity of geometrically nonlinear columns.

In this paper, the authors aimed at shining a light on the behaviour of geometrically nonlinear steel columns and the factors affecting its load-carrying capacity. Two cases were considered: a

curved column and a Y shaped single armed column. These columns were modelled using a validated FE model that was created using Abaqus. Using this model, the effects of three factors were studied on the load-carrying capacity of the columns. These factors were:

A. Length: For the curved columns the length of the entire column was considered. For the Y shaped columns, the length of inclined part was considered.

B. The effects of support conditions.

C. The effects of the included angle (i.e., changing depth/reach ratio).

D. After the parametric studies were carried out, the following was observed:

E. The two cases that were chosen to be studied were behaving significantly different to each other. For instance, changing the included angle for curved columns from 55 to 35 results in a capacity reduction of over 55%, whereas changing the angle from 60 to 40 in Y shaped column results in 40% reduction (see Figures 8 & 9). It was also noticed that curved columns and Y shaped columns start exhibiting nonlinear behaviour at different stages of their load-carrying capacity. This signifies the importance of carrying out further studies into each type of column independently to avoid any ambiguity and be able to make confident conclusions.

F. The effects of included angle on the load-carrying capacity of nonlinear columns: the results show that this factor affects the capacity of columns significantly. This is similar to studies carried out reading the behaviour of arches previously [8].

G. Boundary conditions were observed to also have an effect on the load-carrying capacity of nonlinear columns as shown in Figures 10 & 11. Columns that were modelled as free at the top end were observed to fail in out of plane buckling. This is a similar behaviour to steel arches investigated by previous studies [21].

H. Effects of length: for the curved columns, the modelled columns reached their section capacity before displaying nonlinear behaviour. Y shaped columns, on the other hand, started displaying nonlinear behaviour at about 70% of their capacity load. This has been shown in Figures 12 & 13.

Current design codes do not, to the knowledge of the authors, explicitly state a formula for design of geometrically nonlinear columns. What is provided is guidance on the design of steel members which are curved in the plane of loading. This has been discussed in section 5 of this paper.

Having shown, in the results, the similarities in behaviour of nonlinear column to that of arches, it can be concluded that the design curves produced for arches can be utilised, with a great degree of confidence, to estimate the load-carrying capacity of nonlinear columns.

Nonetheless, it is important to remember that that the available design formulas and curves are produced for the design of arches. These cannot be used for the design of nonlinear columns without any correction. These charts can be used as a basis for developing formulas specific to nonlinear columns, after allowing for appropriate corrections.

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