

Tipping Bucket Rain Gauge Performance Analysis under Heavy Rainfall

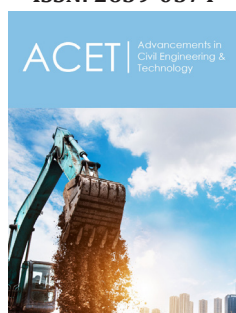
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Abstract

Rainfall index has become the most important index in all rainfall-induced natural disaster. Rainfall intensity in 5 or 10 minutes, accumulated rainfall amount in 1 hour to 24 hours are most used index. The dominate rainfall data comes from wide distributed traditional rainfall gauge. Although rainfall radars are used and considered to be better than traditional rainfall gauge, but Radar data still needs rain gauge data for calibration and justification. The dominant type of rain gauge is the tipping bucket rain gauge (TBR). This research derived the error and accuracy of TBR. The equations of motion were derived through the conservation of linear momentum and angular momentum. An initial value problem was obtained, and the input rainfall was calculated using the 4th order Runge-Kutta method. The result of the theory was compared with ISO/IEC 17025 certified indoor experiments with an error less than 1%. Then the result is compared with field measurement. It is found that high-intensity rainfall is usually underestimated from readings of tipping bucket rain gauge. The TBR underestimated rainfall by 20% when rainfall intensity reached 100 mm/hr.

Keywords: Tipping bucket rain gauge; High rainfall intensity

Introduction

Rainfall data is one of the most important data in meteorology, hydrology, water resource, and natural hazards. The observed rainfall data describes weather characteristic and uses for meteorological models' calibration from short-term rainfall forecast (1-7 days) to long-term projected climate (10-100 years). The rainfall data is also a critical input for simulations of hydrological processes and rainfall-triggered natural hazards in watersheds. For hydrological modelling such as runoff, flow discharge, and groundwater, they can further affect the water resource operation for reservoirs and water usage policies for agriculture, industry, and local people. For natural hazards simulations such as landslides, debris flows, and flooding, they can strongly influence the countermeasures, evacuation routes, and other disaster prevention policies. Besides, the rainfall amount in 1 hr. or 24 hrs. (intensity, accumulated rainfall) and duration are frequently used index for warning of landslides or debris flows [1-3] all over the world. The rain gauge data is considered to be crucial for a wide variety of usages as well as influenced the interpretation of research results.

There are several types of rain gauge in practice, traditional or radar. Doppler rainfall radar systems are considered to be better than traditional mechanical rainfall gauge because it can obtain rainfall data in a large area. But Radar data needs ground mechanical rain gauge data for calibration and justification. The most used mechanical rain gauge is tipping bucket rain gauge (TBR) [4]. The resolution of the TBR is decided by the maximum water capacity (nominal volume) of one bucket. When the inflow rainwater is greater than the nominal volume in one side, the buckets will tip from one side to the other and record one nominal column at the same time. In this design, the loss of rain volume usually appears during the finite time of the tipping movement of buckets (disregard the environmental factors). This loss usually increases in a non-linear increment of rainfall intensity and always results in the under catch of the actual amount of rain [5-7], especially in high rainfall intensity. For example, in indoor experiments, the underestimated rainfall measured by 0.1, 0.2, 0.5, 1mm resolution TBR can reach 37%, 30%, 15%, 8% respectively when rainfall intensity reaches

600mm/hr. [8]. Therefore, the observed records of the TBR should be corrected for actual amount of rain. Furthermore, the maxima detectable rainfall intensity for the TBR in different resolution should be defined as well.

To modify the TBR records, the experiments calibration was usually applied in past studies. There is no theory has been developed to predict rainfall by simulating the dynamic movement of tipping buckets. This research provided a theory to describe the dynamic tipping movement of the buckets. The theory was derived through the conservation of linear momentum and angular momentum step by step in section 2. With the proposed theory, the transient tipping process was simulated and validated with indoor

experiments. The performance of the TBR and its application range of rainfall intensity was discussed as well.

Fundamental Theory

In TBR design, the mechanical process can separate into two stages: 1) stationary stage and 2) buckets rotation stage. In first stage, the buckets are stationary until the filled rainwater greater than the nominal volume in one side of the buckets. As the increased water level, the center of water mass gradually moves away from the pivot. The free body diagram for single bucket is shown in Figure 1. Because the system of the buckets still at rest, the static equilibrium in each time steps can be solved through the simple force balance and moment balance (Table 1). The static equilibrium in 2D are

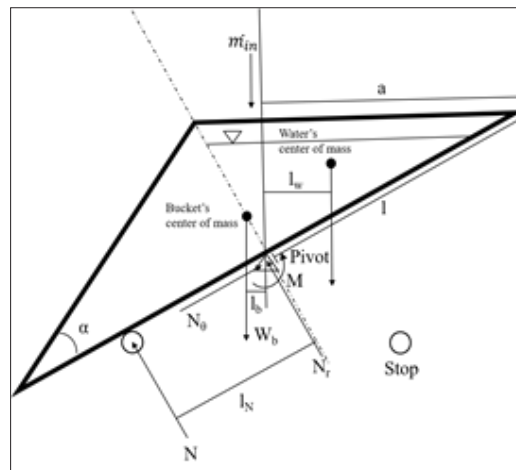


Figure 1: Free body diagram of a single bucket.

Table 1: Lists of Symbols.

Symbols	Meaning
N_r, N_θ	Reaction on pivot in r - and θ - direction
N	Reaction on stop
M	Friction Moment on pivot
W_b, W_w	Body force of buckets and water
l_N, l_w, l_b	Moment arm of stop, water, and buckets
g	Acceleration of gravity
ρ_b, ρ_w	Density of buckets and water
$\dot{m}_{in}, \dot{m}_{out}$	Mass flux of inflow and outflow
V_{full}, V_{unit}	Maximum and nominal volume of one bucket
α	Interior angle of buckets
r_b, r_w	The distance from origin to center mass of buckets and water
$\theta_b, \theta_w, \theta_{out}$	Angle between reference axis and \vec{r}_b, \vec{r}_w and
v_{in}, v_{out}	Inflow and outflow velocity

Force balance

$$N + N_r = (W_b + W_w) \cos \alpha, \tag{1}$$

$$N_\theta = (W_w + W_b) \sin \alpha, \tag{2}$$

Moment balance

$$N \cdot l_N + W_w \cdot l_w - W_b \cdot l_b - M = 0, \tag{3}$$

The conservative of mass

$$\dot{m}_{in} \cdot t = \rho_w \cdot Q_{in} \cdot t = \frac{W_w}{g}, \tag{4}$$

and the geometric relationship gives the distance l_w in

$$l_w = \frac{2}{3} (l \cos \alpha - 0.5a) \cdot \sqrt{\frac{Q_{in} \cdot t}{V_{full}}}. \tag{5}$$

By applying virtual work,

$$\sqrt{\frac{Q_{in} \cdot t}{V_{full}}} l \cos \alpha \cdot W_w - l_b \sec^2 \alpha \cdot W_b + l_N \sec^2 \alpha \cdot N - M = 0 \tag{6}$$

$$N = \left[W_b l_b \tan^2 \alpha - \frac{W_w}{3} (l \cos \alpha + a) \sqrt{\frac{Q_{in} \cdot t}{V_{full}}} \right] (l_N \tan^2 \alpha)^{-1} \tag{7}$$

we can solve all the unknowns as

$$N_r = (W_b + W_w) \cos \alpha - N, \tag{8}$$

$$N_\theta = (W_b + W_w) \sin \alpha, \tag{9}$$

$$M = N \cdot l_N + W_w \cdot l_w - W_b \cdot l_b. \tag{10}$$

This provides the equilibrium condition when the bucket is stationary. When there is just enough rainfall to initialize the bucket

motion, it is when $Q_{in} \cdot t = V_{unit}$. So, all forces at the initial of motion are

$$N = \left[W_b l_b (1 + \sec^2 \alpha) + \rho g V_{unit} \sqrt{\frac{V_{unit}}{V_{full}}} l \frac{\cos \alpha + a}{3} \right] \left[l_N (1 + \sec^2 \alpha) \right]^{-1} \quad (11)$$

$$N_r = (W_b + W_w) \cos \alpha - N \quad (12)$$

$$N_\theta = (W_b + W_w) \sin \alpha \quad (13)$$

$$M = \rho g V_{unit} \sqrt{\frac{V_{unit}}{V_{full}}} l \cos \alpha + l_b W_b \cos \alpha - l_N \sec^2 \alpha \cdot N \quad (14)$$

After this condition is satisfied, we should move from static equilibrium to dynamic equilibrium. The buckets start to revolve around the pivot and the filled water start to flow out. The new force balance is depicted in Figure 2.

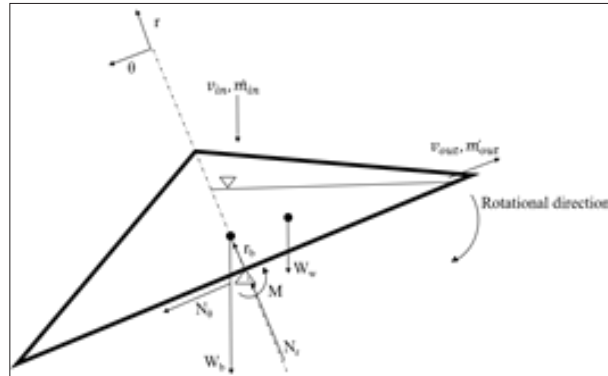


Figure 2: A sketch of dynamic motion.

Since the water is flowing out, the whole system can be regarded as variable mass system. The mass conservation is

$$m \frac{d\bar{v}}{dt} = \sum \bar{F} + \bar{v}' \frac{dm}{dt} \quad (15)$$

Linear momentum conservation equations are

$$m_b (-r_b \dot{\theta}_b^2) = N_r - W_w \sin \theta_b - W_b \sin \theta_b - \dot{m}_{in} v_{in} \sin \theta_b - \dot{m}_{out} v_{out} \cos(\theta_b - \theta_{out}) \quad (16)$$

$$m_b r_b \ddot{\theta}_b = N_\theta - W_w \cos \theta_b - W_b \cos \theta_b + \sin(-v_{in} \cos \theta_b + v_b) - \dot{m}_{out} (-v_{out} \cos(\theta_b - \theta_{out}) + v_b) \quad (17)$$

and angular momentum conservation is

$$I_b \frac{d^2 \theta_b}{dt^2} = -M - W_b r_b \cos \theta_b + W_w r_w \cos \theta_w \quad (18)$$

During rotating movement, it can be proved that the free surface remains horizontal. After summarizing all equations (16)~(18) and let most of variables substitute for known parameter. We could have these three equations.

$$N_r = -m_b r_b \dot{\theta}_b^2 + 0.5 \rho_w g B l^2 (\tan(\beta + \theta_b) \sin + \dot{\theta}_b \sec^2(\beta + \theta_b) v_{out} \cos(\theta_b - \theta_{out})) + W_b \sin \theta_b + m_{in} v_{in} \sin \theta_b \quad (19)$$

$$N_\theta = m_b r_b \ddot{\theta}_b + 0.5 \rho_w g B l^2 [\tan(\beta + \theta_b) \cos \theta_b + \dot{\theta}_b \sec^2(\beta + \theta_b) (r_b \dot{\theta}_b - v_{out} \sin(\theta_b - \theta_{out}))] + W_b \cos \theta_b + \dot{m}_{in} (v_{in} \cos \theta_b - v_{out} \sin(\theta_b - \theta_{out})) \quad (20)$$

$$I_b \frac{d^2 \theta_b}{dt^2} = -M - W_b r_b \cos \theta_b + 0.5 \rho_w g B l^2 \tan(\beta + \theta_b) \frac{l}{3} \cos(2\beta + 2\theta_b) \quad (21)$$

l_b is the location of the center of mass of bucket and is solved from (21) as a function of time? (19), (20) and (21) are solved with 4th order Runge-Kutta method. The initial conditions are Eq. (12) to (14). The variation of l_b indicates the movement of the bucket and can be compared with experiments.

Simulation and Validation

To validate the proposed theory, the widely used TBR by Water Resource Agency in Taiwan (model: TK-1 rain gauge) was selected

for test. In this experiment, the outer shell, rainfall collector, was removed for clear observation. A steady rainfall intensity was supplied using a fixed head inflow device, as shown in Figure 2. The TBR rain gauge was put in a tank and weighed by an electronic scale. With this design, the weight of inflow water can be recorded with time. The recordings of weight in buckets were calculated for validation of reaction forces. Besides, a video camera (~30 fps) was used to record the motion of bucket and the actual rotating angle of buckets was measured through video snapshots, as listed in Table 2. All these experiment setups are certified by ISO/IEC 17025 standard. Under rainfall intensity of 100mm/hr, the variation of rotation angle was simulated using Eq. (19)~(21) with initial condition of Eq. (12)~(14), as depicted in Figure 3. Compared to the experiment result, the maximum error of simulated rotation angle is less than 1%. The simulated result is in a good agreement with the measured one.

Table 2: Rotating angle of buckets caught by video camera.

Time (sec.)	Angle θ_b (degree)	Time (sec.)	Angle θ_b (degree)
0.03	120	0.33	115.2
0.06	119.6	0.36	113.8
0.09	119.2	0.39	111.8
0.12	119	0.42	109
0.15	118.9	0.45	104.7
0.18	118.5	0.48	99.8
0.21	118	0.51	92.4
0.24	117.3	0.54	83.5
0.27	117	0.57	73.2
0.3	116	0.6	66

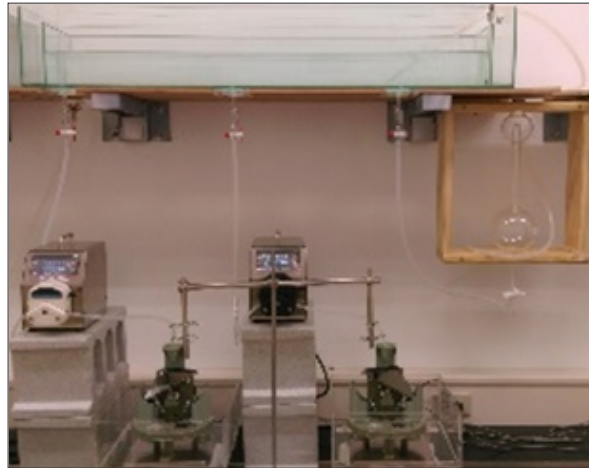


Figure 3: Experimental setup of tipping bucket and fixed head inflow device.

Conclusion

This research used fluid mechanics and dynamics to solve the TBR motion. The governing equations divide by two parts: static part and dynamic part. Static part governs by equations of equilibrium and virtual work method. Dynamic part governs by Navier-Stokes equations, conservative of angular momentum and continuity equation. The 4th order Runge-Kutta method was used to solve the system equations. Indoor experiments were used for validation. The theoretical value is very close to indoor experiments with error less than 1%. The simulation result shows that tipping time of 1mm TBR such as TK-1 rain gage takes about 0.6 second. In this 0.6 second, tipping side is still catching water about 0.4 second. It means when the bucket tips, it'll lost about 0.4 seconds rainfall data. This error will increase with increasing rainfall intensity. When rainfall intensity reaches 100mm/hr., the lost water amount during the lost 0.4s is 20%. Considering rainfall rarely distributed uniformly in time, a 100mm/hr. intensity usually means intensity is much larger in a shorter duration within that hour. Therefore, the actual error should be larger.

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