Radial Basis Function Network versus Regression Model in Manufacturing Processes Prediction

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Abstract
One of the objectives of manufacturing industry, is to increase the efficiency in their processes using different methodologies, such as statistical modeling, for production control and decision-making. However, the classical tools sometimes have difficulty to depict the manufacturing processes. This paper is a comparative study between a multiple regression model and a Radial Basis Function Neural Network in terms of the statistical metrics $R^2$ and $R^2_{adj}$ applied in a permanent mold casting process and TIG welding process. Results showed that in both cases, the RBF network performed better than Regression model.

Keywords: Radial basis function; Multiple regression; Process prediction

Introduction
Nowadays, the manufacturing companies have been increased difficulty in their process decision making, due to rapid changes in design methods and demand for quality products [1]. For that reason, there are different tools for modeling a process, like statistical, mathematical and intelligent systems, but the question is which of these tools depict better the process?

The multiple regression is a statistical model that analyze how a set of predictor variables $X$ are related to a single response measured $y$. Regression analysis answers questions about the dependence of a single response variable on one or more predictors, including prediction of future values, discovering which predictors are important and estimating the impact of changing a predictor or a treatment on the value of the response [2]. The Radial Basis Function (RBF) neural network aids to explain the process outputs based on the inputs assigned to it. For example, to automate a manufacturing process, it is necessary to know the input-output relationship in both directions, and using a radial basis network it is possible to predict the results of a manufacturing process efficiently [3]. The RBF networks are important in prediction by his character of universal approximators [4] and for its good performance in the non-linearity common in processes [5]. In this paper, we propose a comparative study between a multiple regression model and a Radial Basis Function Neural Network in terms of the statistical metrics $R^2$, $R^2_{adj}$, $R^2_{PRESS}$ applied in a permanent mold casting process.

Methods

Radial basis function network
Are so called Radial basis functions because the functions of the hidden layer as a base set for the function to be approximated, and the functions display a radial symmetry, being only a function of the distance between the learned patterns and the input ones.

A neural network with radial basis function consists of the following layers [6]:

Input layer: it is formed by the source nodes (sensory units).

Intermediate layer: it is a hidden layer of great dimension and in which the units (neurons) that form it are the base functions for the input data.

Output layer: that has the responsibility in the network for the activation of patterns applied in the input layer.

Radial basis functions are functions that reach a level close to the maximum of their path when the input pattern ($X^0$) is close to the center of the neuron. If the pattern moves away from the center, the value of the function tends to the minimum value of its path. The training is only forward. The output of a network in general is influenced by a non-linear transformation, originating in the hidden layer through the radial function and a linear one in the output layer through the continuous linear function. A derivation
of the radial basis models is the use of the standard deviation to activate the function $G(*)$, working with $\exp(d^2 / a^2)$, where $a$ is the standard deviation for the hidden node.

**Genetic algorithm**

As mentioned above, the RBF output depends on the distance between the inputs to the network centers. There are many methods of clustering and optimization for determining the centers. One of them is the Genetic Algorithm (GA), which is a method of optimization based on the processes of biological evolution [7]. It is part of intelligent systems.

The process consists in select randomly individuals of the current population; these individuals will be the parents of the next generation that will be evolve to an optimal solution. The GA works on three main rules [8]:

- Parent selection of the next generation.
- The combination of parents to form the next generation.
- Applying random changes of each parent for the children.

The GA considers one function of evaluation (fitness function) to optimize. The objective is maximizing or minimizing such fitness function. Applying GA to determine the centroids of the RBF, the metric used is $R^2$ which is a global evaluation metric [9], in this case the objective is to maximize this metric.

**Multiple regression**

A regression model which involves more than one regressor variable is called multiple regression model. In general, you can relate a response $Y$ with $k$ regressors or predictors. The statistical model to explain the behavior of the dependent variable including any number of independent variables is equation (1).

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_k X_k + \varepsilon_i \quad (1)$$

The deviation of an observation $Y_i$ from its population mean $E[Y_i]$ is taken into account by adding a random error $E_i$. There are $k$ independent variables and $k+1$ parameters to be estimated. Usually, the estimation of the parameters $\beta_j$ is made by means of the Ordinary least Square Method (OLS). In a matrix form, the OLS estimator is given by [9]:

$$\hat{Y} = \hat{\beta} X + \varepsilon$$

The statistical model above can be expressed in matrix form as:

$$\begin{bmatrix} Y_1 \\ Y_2 \\ \vdots \\ Y_n \end{bmatrix} = \begin{bmatrix} 1 & X_1 & \cdots & X_k \end{bmatrix} \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_k \end{bmatrix} + \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_n \end{bmatrix}$$

The ordinary least squares (OLS) estimator is:

$$\hat{\beta} = (X'X)^{-1}X'Y$$

**Application**

![Figure 1: Radial basis function structure.](image1)

![Figure 2: Target vs regression.](image2)
The process consists of a permanent mold casting for manufacturing a piece for the electrical industry. They have three independent variables in eight runs. The data were obtained using a factorial design with 3 factors 2 levels. The objective of the modeling is to find the variable that causes more defects and minimize them. The model response is the total defects in the process. The observations are shown in Table 1. The comparison between the real responses and the Regression model is showed in the Figure 1 and the comparison between Radial Basis Function and real response is showed in the Figure 2 & 3.

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<thead>
<tr>
<th>Metal Temperature</th>
<th>Oven Temperature</th>
<th>Tilt Speed</th>
<th>Total Defects</th>
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<tr>
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<td>390</td>
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<td>24</td>
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<tr>
<td>790</td>
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<th>Table 2: Comparison of association measurements.</th>
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<td>R²</td>
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<td>R² adj</td>
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<td>R² adj</td>
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It is possible to see graphically the FBR network model has a better fit than by regression. After that, the measurements of association were estimated to test the performance of a Regression model and RBF. Results are shown in Table 2. It is observed at Table 2, that the RBF Network depicts the process variation over that 90% in terms of the coefficients of determination. The method was applied in the TIG welding process too, using a welding robot Kuka KR-16, with multi-process welding system (MIG and TIG). Then taking process data and identifying the important parameters: feed rate (IPM), input voltage (volts), wire speed (m/min), and the output, the fusion 2 of the welding.

The Figure 4 shows the response called Fusion 2, and measures the penetration of the vertical element to be attached to the horizontal element. This response is important in the material properties since its control depends on the strength of the joint. The Table 3 illustrates the results about the application and comparison between the RBF with Regression model. Those metrics are quantities used to express the proportion of total variability in the response accounted by the model. So that indicates the proportion of variability in yexplained by the model. Then the RBF is better than multivariate regression model.
Conclusion

In order to improve manufacturing processes, it is very important to analyze the process to take better decisions. In this article it was shown that a tool based alternative intelligent systems, generates a better fit compared to regression analysis in terms of the measures of association. This statistical metrics provide information about the strength of the relationships between predictors and the dependent variable. With these results, it is possible to find the parameters that cause more defects. However, for future work is proposed to consider analyze each defect in a model for joint prediction, considering that the model design must be made multivariate: what will happen with the Regression model and RBF?

References